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| <b>Course Code</b>  | <b>EM 212</b>      |  |  |
| <b>Course Title</b>   | <b>Calculus II</b> |  |  |
| <b>No. of Credits</b>   | <b>2</b>           |  |  |
| <b>Pre-requisites</b>   | <b>None</b>        |  |  |
| <b>Compulsory/Optional</b>  | <b>Compulsory</b>  |  |  |
| <p><b>Aim(s):</b> To introduce, calculus of functions of several variables, vector valued functions and the use of integral theorems in any orthogonal curvilinear coordinates to solve engineering problems.</p>   |                    |  |  |
| <p><b>Intended Learning Outcomes:</b><br/>On successful completion of the course, the students should be able to;</p> <ul style="list-style-type: none"> <li>• Sketch level curves and level surfaces of functions of two and three variables, and sketch their surfaces and solids.</li> <li>• Compute double and triple integrals of scalar functions over any given 2D and 3D regions.</li> <li>• Compute gradient, divergence and curl of a given function using orthogonal curvilinear coordinates and to solve related problems using cylindrical and spherical coordinates.</li> <li>• Evaluate line, surface and volume integrals of continuous scalar and vector fields over a given domain and apply integral theorems.</li> </ul>  |                    |  |  |
| <p><b>Time Allocation (Hours):</b> Lectures 24    Tutorials 4    Practical    Assignments 4</p>   |                    |  |  |
| <p><b>Course content/Course description:</b></p> <ul style="list-style-type: none"> <li>• <b>Functions of several variables:</b> Sketching level curves and level surfaces of functions of two and three variables, sketching surfaces and volumes, limit, and continuity of functions of two and three variables; Tangent planes, gradient vector and directional derivative, scalar line integrals.</li> <li>• <b>Double and Triple Integration:</b> Definitions of double and triple integrals, double and triple integrals over rectangular domains, double and triple integrals over any general domains; cylindrical and spherical polar coordinates, Jacobian and its properties, applications of double and triple integrals (change of coordinates).</li> <li>• <b>Vector Fields and Vector Operators:</b> Scalar fields and vector fields, gradient, divergence and curl and their geometrical and physical interpretations.</li> <li>• <b>Vector and complex line integral:</b> Line integrals of vector valued functions and path independency of line integrals, simply connected domains and conservative vector fields, Cauchy-Riemann equations and line integrals of complex valued functions, complex line integrals over simply connected domains and Cauchy's theorem.</li> </ul> |                    |  |  |

- **Orthogonal curvilinear coordinates, Surface integrals and Integral Theorems:** Greens Theorem on the plane, surface integrals of scalar fields and vector fields; Stokes' theorem and divergence theorem, area and volume elements in terms of orthogonal curvilinear coordinates; Surface integrals with orthogonal curvilinear coordinates, applications of integral theorems in terms of orthogonal curvilinear coordinates.

**Recommended Texts :**

- James Stewart, Calculus, 5<sup>th</sup> edition, (2006), Thomson Books/Cole.
- Watson Fulks, Advanced Calculus an Introduction to Analysis, 3<sup>rd</sup> Edition, (1978), John Wiley & Sons Inc.
- E. B. Saff and A. D. Sinder, Fundamentals of Complex Analysis with Applications to Engineering, Science, and Mathematics, 3rd edition, (2014), Pearson Education Ltd.

| <b>Assessment</b>        | <b>Percentage Mark</b> |
|--------------------------|------------------------|
| <b>In-course</b>         |                        |
| Tutorials                | 10                     |
| Mid Semester Examination | 30                     |
| <b>End-semester</b>      | 60                     |